

## CHAPTER 2 POLYNOMIALS

### Exercise 2.4

Page: 40

1. Use suitable identities to find the following products:

(i)  $(x+4)(x+10)$

Solution:

Using the identity,  $(x+a)(x+b) = x^2+(a+b)x+ab$

[Here,  $a = 4$  and  $b = 10$ ]

We get,

$$(x+4)(x+10) = x^2+(4+10)x+(4 \times 10)$$

$$= x^2+14x+40$$

(ii)  $(x+8)(x-10)$

Solution:

Using the identity,  $(x+a)(x+b) = x^2+(a+b)x+ab$

[Here,  $a = 8$  and  $b = -10$ ]

We get,

$$(x+8)(x-10) = x^2+(8+(-10))x+(8 \times (-10))$$

$$= x^2+(8-10)x-80$$

$$= x^2 - 2x - 80$$

**(iii)  $(3x+4)(3x-5)$**

Solution:

Using the identity,  $(x+a)(x+b) = x^2 + (a+b)x + ab$

[Here,  $x = 3x$ ,  $a = 4$  and  $b = -5$ ]

We get,

$$(3x+4)(3x-5) = (3x)^2 + [4+(-5)]3x + 4 \times (-5)$$

$$= 9x^2 + 3x(4-5) - 20$$

$$= 9x^2 - 3x - 20$$

**(iv)  $(y^2+3/2)(y^2-3/2)$**

Solution:

Using the identity,  $(x+y)(x-y) = x^2 - y^2$

[Here,  $x = y^2$  and  $y = 3/2$ ]

We get,

$$(y^2+3/2)(y^2-3/2) = (y^2)^2 - (3/2)^2$$

$$= y^4 - 9/4$$

**(v)  $(3+2x)(3-2x)$**

We know that  $(x+y)(x-y) = x^2 - y^2$ .

We need to apply the above identity to find the product  $(3+2x)(3-2x)$

$$(3+2x)(3-2x) = (3)^2 - (2x)^2$$

$$= 9 - 4x^2.$$

Therefore, we conclude that the product  $(3+2x)(3-2x)$  is  $(9-4x^2)$ .

## **2. Evaluate the following products without multiplying directly:**

### **(i) $103 \times 107$**

Solution:

$$103 \times 107 = (100+3) \times (100+7)$$

Using identity,  $[(x+a)(x+b) = x^2 + (a+b)x + ab$

Here,  $x = 100$

$$a = 3$$

$$b = 7$$

$$\text{We get, } 103 \times 107 = (100+3) \times (100+7)$$

$$= (100)^2 + (3+7)100 + (3 \times 7)$$

$$= 10000 + 1000 + 21$$

$$= 11021$$

### **(ii) $95 \times 96$**

Solution:

$$95 \times 96 = (100-5) \times (100-4)$$

Using identity,  $[(x-a)(x-b) = x^2 - (a+b)x + ab]$

Here,  $x = 100$

$$a = -5$$

$$b = -4$$

We get,  $95 \times 96 = (100-5) \times (100-4)$

$$= (100)^2 + 100(-5 + (-4)) + (-5 \times -4)$$

$$= 10000 - 900 + 20$$

$$= 9120$$

### **(iii) 104 × 96**

Solution:

$$104 \times 96 = (100+4) \times (100-4)$$

Using identity,  $[(a+b)(a-b) = a^2 - b^2]$

Here,  $a = 100$

$$b = 4$$

We get,  $104 \times 96 = (100+4) \times (100-4)$

$$= (100)^2 - (4)^2$$

$$= 10000 - 16$$

$$= 9984$$

### 3. Factorise the following using appropriate identities:

**(i)  $9x^2+6xy+y^2$**

Solution:

$$9x^2+6xy+y^2 = (3x)^2+(2\times 3x\times y)+y^2$$

Using identity,  $x^2+2xy+y^2 = (x+y)^2$

Here,  $x = 3x$

$$y = y$$

$$9x^2+6xy+y^2 = (3x)^2+(2\times 3x\times y)+y^2$$

$$= (3x+y)^2$$

$$= (3x+y)(3x+y)$$

**(ii)  $4y^2-4y+1$**

Solution:

$$4y^2-4y+1 = (2y)^2-(2\times 2y\times 1)+1$$

Using identity,  $x^2 - 2xy + y^2 = (x - y)^2$

Here,  $x = 2y$

$$y = 1$$

$$4y^2-4y+1 = (2y)^2-(2\times 2y\times 1)+1^2$$

$$= (2y-1)^2$$

$$= (2y-1)(2y-1)$$

**(iii)  $x^2 - y^2/100$**

Solution:

$$x^2 - y^2/100 = x^2 - (y/10)^2$$

Using identity,  $x^2 - y^2 = (x-y)(x+y)$

Here,  $x = x$

$$y = y/10$$

$$x^2 - y^2/100 = x^2 - (y/10)^2$$

$$= (x - y/10)(x + y/10)$$

**4. Expand each of the following using suitable identities:**

**(i)  $(x+2y+4z)^2$**

**(ii)  $(2x-y+z)^2$**

**(iii)  $(-2x+3y+2z)^2$**

**(iv)  $(3a-7b-c)^2$**

**(v)  $(-2x+5y-3z)^2$**

**(vi)  $((1/4)a - (1/2)b + 1)^2$**

Solution:

**(i)  $(x+2y+4z)^2$**

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

Here,  $x = x$

$$y = 2y$$

$$z = 4z$$

$$(x+2y+4z)^2 = x^2+(2y)^2+(4z)^2+(2 \times x \times 2y)+(2 \times 2y \times 4z)+(2 \times 4z \times x)$$

$$= x^2+4y^2+16z^2+4xy+16yz+8xz$$

**(ii)  $(2x-y+z)^2$**

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

Here,  $x = 2x$

$$y = -y$$

$$z = z$$

$$(2x-y+z)^2 = (2x)^2+(-y)^2+z^2+(2 \times 2x \times -y)+(2 \times -y \times z)+(2 \times z \times 2x)$$

$$= 4x^2+y^2+z^2-4xy-2yz+4xz$$

**(iii)  $(-2x+3y+2z)^2$**

Solution:

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

Here,  $x = -2x$

$$y = 3y$$

$$z = 2z$$

$$\begin{aligned}(-2x+3y+2z)^2 &= (-2x)^2+(3y)^2+(2z)^2+(2 \times -2x \times 3y)+(2 \times 3y \times 2z)+(2 \times 2z \times -2x) \\ &= 4x^2+9y^2+4z^2-12xy+12yz-8xz\end{aligned}$$

$$\text{(iv) } (3a - 7b - c)^2$$

Solution:

Using identity  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

Here,  $x = 3a$

$$y = -7b$$

$$z = -c$$

$$\begin{aligned}(3a - 7b - c)^2 &= (3a)^2+(-7b)^2+(-c)^2+(2 \times 3a \times -7b)+(2 \times -7b \times -c)+(2 \times -c \\ &\times 3a) \\ &= 9a^2 + 49b^2 + c^2 - 42ab + 14bc - 6ca\end{aligned}$$

$$\text{(v) } (-2x+5y-3z)^2$$

Solution:

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

Here,  $x = -2x$

$$y = 5y$$



$$z = -3z$$

$$(-2x+5y-3z)^2 = (-2x)^2+(5y)^2+(-3z)^2+(2 \times -2x \times 5y)+(2 \times 5y \times -3z)+(2 \times -3z \times -2x)$$

$$= 4x^2+25y^2+9z^2- 20xy-30yz+12zx$$

$$\text{(vi) } \left(\frac{1}{4}a - \frac{1}{2}b + 1\right)^2$$

Solution:

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

$$\text{Here, } x = \frac{1}{4}a$$

$$y = -\frac{1}{2}b$$

$$z = 1$$

$$\begin{aligned} \left(\frac{1}{4}a - \frac{1}{2}b + 1\right)^2 &= \left(\frac{1}{4}a\right)^2 + \left(-\frac{1}{2}b\right)^2 + (1)^2 + \left(2 \times \frac{1}{4}a \times -\frac{1}{2}b\right) + \left(2 \times -\frac{1}{2}b \times 1\right) + \left(2 \times 1 \times \frac{1}{4}a\right) \\ &= \frac{1}{16}a^2 + \frac{1}{4}b^2 + 1^2 - \frac{2}{8}ab - \frac{2}{2}b + \frac{2}{4}a \\ &= \frac{1}{16}a^2 + \frac{1}{4}b^2 + 1 - \frac{1}{4}ab - b + \frac{1}{2}a \end{aligned}$$

**5. Factorise:**

$$\text{(i) } 4x^2+9y^2+16z^2+12xy-24yz-16xz$$

$$\text{(ii) } 2x^2+y^2+8z^2-2\sqrt{2}xy+4\sqrt{2}yz-8xz$$

Solution:

$$\text{(i) } 4x^2+9y^2+16z^2+12xy-24yz-16xz$$

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

We can say that,  $x^2+y^2+z^2+2xy+2yz+2zx = (x+y+z)^2$

$$4x^2+9y^2+16z^2+12xy-24yz-16xz =$$

$$(2x)^2+(3y)^2+(-4z)^2+(2 \times 2x \times 3y)+(2 \times 3y \times -4z)+(2 \times -4z \times 2x)$$

$$= (2x+3y-4z)^2$$

$$= (2x+3y-4z)(2x+3y-4z)$$

**(ii)  $2x^2+y^2+8z^2-2\sqrt{2}xy+4\sqrt{2}yz-8xz$**

Using identity,  $(x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$

We can say that,  $x^2+y^2+z^2+2xy+2yz+2zx = (x+y+z)^2$

$$2x^2+y^2+8z^2-2\sqrt{2}xy+4\sqrt{2}yz-8xz$$

$$= (-\sqrt{2}x)^2+(y)^2+(2\sqrt{2}z)^2+(2 \times -\sqrt{2}x \times y)+(2 \times y \times 2\sqrt{2}z)+(2 \times 2\sqrt{2} \times -\sqrt{2}x)$$

$$= (-\sqrt{2}x+y+2\sqrt{2}z)^2$$

$$= (-\sqrt{2}x+y+2\sqrt{2}z)(-\sqrt{2}x+y+2\sqrt{2}z)$$

**6. Write the following cubes in expanded form:**

**(i)  $(2x+1)^3$**

**(ii)  $(2a-3b)^3$**

**(iii)  $((\frac{3}{2})x+1)^3$**

**(iv)  $(x-(\frac{2}{3})y)^3$**

Solution:

**(i)  $(2x+1)^3$**

Using identity,  $(x+y)^3 = x^3+y^3+3xy(x+y)$

$$(2x+1)^3 = (2x)^3+1^3+(3 \times 2x \times 1)(2x+1)$$

$$= 8x^3+1+6x(2x+1)$$

$$= 8x^3+12x^2+6x+1$$

**(ii)  $(2a-3b)^3$**

Using identity,  $(x-y)^3 = x^3-y^3-3xy(x-y)$

$$(2a-3b)^3 = (2a)^3-(3b)^3-(3 \times 2a \times 3b)(2a-3b)$$

$$= 8a^3-27b^3-18ab(2a-3b)$$

$$= 8a^3-27b^3-36a^2b+54ab^2$$

**(iii)  $\left(\frac{3}{2}x+1\right)^3$**

Using identity,  $(x+y)^3 = x^3+y^3+3xy(x+y)$

$$\left(\frac{3}{2}x+1\right)^3 = \left(\frac{3}{2}x\right)^3+1^3+(3 \times \frac{3}{2}x \times 1)\left(\frac{3}{2}x+1\right)$$

$$\begin{aligned} &= \frac{27}{8}x^3+1+\frac{9}{2}x\left(\frac{3}{2}x+1\right) \\ &= \frac{27}{8}x^3+1+\frac{27}{4}x^2+\frac{9}{2}x \\ &= \frac{27}{8}x^3+\frac{27}{4}x^2+\frac{9}{2}x+1 \end{aligned}$$

**(iv)  $(x-\frac{2}{3}y)^3$**

Using identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$

$$\begin{aligned} \left(x - \frac{2}{3}y\right)^3 &= \left(x\right)^3 - \left(\frac{2}{3}y\right)^3 - \left(3 \times x \times \frac{2}{3}y\right)\left(x - \frac{2}{3}y\right) \\ &= \left(x\right)^3 - \frac{8}{27}y^3 - 2xy\left(x - \frac{2}{3}y\right) \\ &= \left(x\right)^3 - \frac{8}{27}y^3 - 2x^2y + \frac{4}{3}xy^2 \end{aligned}$$

**7. Evaluate the following using suitable identities:**

**(i)  $(99)^3$**

**(ii)  $(102)^3$**

**(iii)  $(998)^3$**

Solutions:

**(i)  $(99)^3$**

Solution:

We can write 99 as  $100 - 1$

Using identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$

$$(99)^3 = (100 - 1)^3$$

$$= (100)^3 - 1^3 - (3 \times 100 \times 1)(100 - 1)$$

$$= 1000000 - 1 - 300(100 - 1)$$

$$= 1000000 - 1 - 30000 + 300$$

$$= 970299$$

**(ii)  $(102)^3$**

Solution:

We can write 102 as  $100+2$

Using identity,  $(x+y)^3 = x^3+y^3+3xy(x+y)$

$$(100+2)^3 = (100)^3+2^3+(3 \times 100 \times 2)(100+2)$$

$$= 1000000 + 8 + 600(100 + 2)$$

$$= 1000000 + 8 + 60000 + 1200$$

$$= 1061208$$

**(iii)  $(998)^3$**

Solution:

We can write 99 as  $1000-2$

Using identity,  $(x-y)^3 = x^3-y^3-3xy(x-y)$

$$(998)^3 = (1000-2)^3$$

$$= (1000)^3-2^3-(3 \times 1000 \times 2)(1000-2)$$

$$= 1000000000-8-6000(1000-2)$$

$$= 1000000000-8-6000000+12000$$

$$= 994011992$$

**8. Factorise each of the following:**

**(i)  $8a^3+b^3+12a^2b+6ab^2$**

**(ii)  $8a^3-b^3-12a^2b+6ab^2$**

**(iii)  $27-125a^3-135a+225a^2$**

**(iv)  $64a^3-27b^3-144a^2b+108ab^2$**

**(v)  $27p^3-(1/216)-(9/2)p^2+(1/4)p$**

Solutions:

**(i)  $8a^3+b^3+12a^2b+6ab^2$**

Solution:

The expression,  $8a^3+b^3+12a^2b+6ab^2$  can be written as

$$(2a)^3+b^3+3(2a)^2b+3(2a)(b)^2$$

$$8a^3+b^3+12a^2b+6ab^2 = (2a)^3+b^3+3(2a)^2b+3(2a)(b)^2$$

$$= (2a+b)^3$$

$$= (2a+b)(2a+b)(2a+b)$$

Here, the identity,  $(x+y)^3 = x^3+y^3+3xy(x+y)$  is used.

**(ii)  $8a^3-b^3-12a^2b+6ab^2$**

Solution:

The expression,  $8a^3-b^3-12a^2b+6ab^2$  can be written as  $(2a)^3-b^3-$

$$3(2a)^2b+3(2a)(b)^2$$

$$8a^3 - b^3 - 12a^2b + 6ab^2 = (2a)^3 - b^3 - 3(2a)^2b + 3(2a)(b)^2$$

$$= (2a - b)^3$$

$$= (2a - b)(2a - b)(2a - b)$$

Here, the identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$  is used.

**(iii)  $27 - 125a^3 - 135a + 225a^2$**

Solution:

The expression,  $27 - 125a^3 - 135a + 225a^2$  can be written as  $3^3 - (5a)^3 -$

$$3(3)^2(5a) + 3(3)(5a)^2$$

$$27 - 125a^3 - 135a + 225a^2 =$$

$$3^3 - (5a)^3 - 3(3)^2(5a) + 3(3)(5a)^2$$

$$= (3 - 5a)^3$$

$$= (3 - 5a)(3 - 5a)(3 - 5a)$$

Here, the identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$  is used.

**(iv)  $64a^3 - 27b^3 - 144a^2b + 108ab^2$**

Solution:

The expression,  $64a^3 - 27b^3 - 144a^2b + 108ab^2$  can be written as  $(4a)^3 - (3b)^3 -$

$$3(4a)^2(3b) + 3(4a)(3b)^2$$

$$\begin{aligned}
&64a^3 - 27b^3 - 144a^2b + 108ab^2 = \\
&(4a)^3 - (3b)^3 - 3(4a)^2(3b) + 3(4a)(3b)^2 \\
&= (4a - 3b)^3 \\
&= (4a - 3b)(4a - 3b)(4a - 3b)
\end{aligned}$$

Here, the identity,  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$  is used.

**(v)  $27p^3 - (1/216) - (9/2)p^2 + (1/4)p$**

Solution:

The expression,  $27p^3 - (1/216) - (9/2)p^2 + (1/4)p$  can be written as

$$(3p)^3 - (1/6)^3 - (9/2)p^2 + (1/4)p = (3p)^3 - (1/6)^3 - 3(3p)(1/6)(3p - 1/6)$$

Using  $(x - y)^3 = x^3 - y^3 - 3xy(x - y)$

$$27p^3 - (1/216) - (9/2)p^2 + (1/4)p = (3p)^3 - (1/6)^3 - 3(3p)(1/6)(3p - 1/6)$$

Taking  $x = 3p$  and  $y = 1/6$

$$= (3p - 1/6)^3$$

$$= (3p - 1/6)(3p - 1/6)(3p - 1/6)$$

**9. Verify:**

**(i)  $x^3 + y^3 = (x + y)(x^2 - xy + y^2)$**

**(ii)  $x^3 - y^3 = (x - y)(x^2 + xy + y^2)$**

Solutions:



$$(i) x^3+y^3 = (x+y)(x^2-xy+y^2)$$

We know that,  $(x+y)^3 = x^3+y^3+3xy(x+y)$

$$\Rightarrow x^3+y^3 = (x+y)^3 - 3xy(x+y)$$

$$\Rightarrow x^3+y^3 = (x+y)[(x+y)^2 - 3xy]$$

Taking  $(x+y)$  common  $\Rightarrow x^3+y^3 = (x+y)[(x^2+y^2+2xy) - 3xy]$

$$\Rightarrow x^3+y^3 = (x+y)(x^2+y^2-xy)$$

$$(ii) x^3-y^3 = (x-y)(x^2+xy+y^2)$$

We know that,  $(x-y)^3 = x^3-y^3-3xy(x-y)$

$$\Rightarrow x^3-y^3 = (x-y)^3 + 3xy(x-y)$$

$$\Rightarrow x^3-y^3 = (x-y)[(x-y)^2 + 3xy]$$

Taking  $(x-y)$  common  $\Rightarrow x^3-y^3 = (x-y)[(x^2+y^2-2xy) + 3xy]$

$$\Rightarrow x^3-y^3 = (x-y)(x^2+y^2+xy)$$

**10. Factorise each of the following:**

$$(i) 27y^3+125z^3$$

$$(ii) 64m^3-343n^3$$

Solutions:

$$(i) 27y^3+125z^3$$

The expression,  $27y^3+125z^3$  can be written as  $(3y)^3+(5z)^3$

$$27y^3+125z^3 = (3y)^3+(5z)^3$$

We know that,  $x^3+y^3 = (x+y)(x^2-xy+y^2)$

$$27y^3+125z^3 = (3y)^3+(5z)^3$$

$$= (3y+5z)[(3y)^2-(3y)(5z)+(5z)^2]$$

$$= (3y+5z)(9y^2-15yz+25z^2)$$

### **(ii) $64m^3-343n^3$**

The expression,  $64m^3-343n^3$  can be written as  $(4m)^3-(7n)^3$

$$64m^3-343n^3 =$$

$$(4m)^3-(7n)^3$$

We know that,  $x^3-y^3 = (x-y)(x^2+xy+y^2)$

$$64m^3-343n^3 = (4m)^3-(7n)^3$$

$$= (4m-7n)[(4m)^2+(4m)(7n)+(7n)^2]$$

$$= (4m-7n)(16m^2+28mn+49n^2)$$

### **11. Factorise: $27x^3+y^3+z^3-9xyz$ .**

Solution:

The expression  $27x^3+y^3+z^3-9xyz$  can be written as  $(3x)^3+y^3+z^3-3(3x)(y)(z)$

$$27x^3+y^3+z^3-9xyz = (3x)^3+y^3+z^3-3(3x)(y)(z)$$

We know that,  $x^3+y^3+z^3-3xyz = (x+y+z)(x^2+y^2+z^2-xy-yz-zx)$

$$27x^3+y^3+z^3-9xyz = (3x)^3+y^3+z^3-3(3x)(y)(z)$$

$$= (3x+y+z)[(3x)^2+y^2+z^2-3xy-yz-3xz]$$

$$= (3x+y+z)(9x^2+y^2+z^2-3xy-yz-3xz)$$

**12. Verify that:**

$$x^3+y^3+z^3-3xyz = (1/2)(x+y+z)[(x-y)^2+(y-z)^2+(z-x)^2]$$

Solution:

We know that,

$$x^3+y^3+z^3-3xyz = (x+y+z)(x^2+y^2+z^2-xy-yz-xz)$$

$$\Rightarrow x^3+y^3+z^3-3xyz = (1/2)(x+y+z)[2(x^2+y^2+z^2-xy-yz-xz)]$$

$$= (1/2)(x+y+z)(2x^2+2y^2+2z^2-2xy-2yz-2xz)$$

$$= (1/2)(x+y+z)[(x^2+y^2-2xy)+(y^2+z^2-2yz)+(x^2+z^2-2xz)]$$

$$= (1/2)(x+y+z)[(x-y)^2+(y-z)^2+(z-x)^2]$$

**13. If  $x+y+z = 0$ , show that  $x^3+y^3+z^3 = 3xyz$ .**

Solution:

We know that,

$$x^3+y^3+z^3-3xyz = (x+y+z)(x^2+y^2+z^2-xy-yz-xz)$$

Now, according to the question, let  $(x+y+z) = 0$ ,

$$\text{Then, } x^3+y^3+z^3-3xyz = (0)(x^2+y^2+z^2-xy-yz-xz)$$

$$\Rightarrow x^3+y^3+z^3-3xyz = 0$$

$$\Rightarrow x^3+y^3+z^3 = 3xyz$$

Hence Proved

**14. Without actually calculating the cubes, find the value of each of the following:**

**(i)  $(-12)^3+(7)^3+(5)^3$**

**(ii)  $(28)^3+(-15)^3+(-13)^3$**

Solution:

**(i)  $(-12)^3+(7)^3+(5)^3$**

Let  $a = -12$

$b = 7$

$c = 5$

We know that if  $x+y+z = 0$ , then  $x^3+y^3+z^3=3xyz$ .

Here,  $-12+7+5=0$

$$(-12)^3+(7)^3+(5)^3 = 3xyz$$

$$= 3 \times -12 \times 7 \times 5$$

$$= -1260$$

**(ii)  $(28)^3+(-15)^3+(-13)^3$**

Solution:

$$(28)^3 + (-15)^3 + (-13)^3$$

$$\text{Let } a = 28$$

$$b = -15$$

$$c = -13$$

We know that if  $x+y+z = 0$ , then  $x^3+y^3+z^3 = 3xyz$ .

$$\text{Here, } x+y+z = 28-15-13 = 0$$

$$(28)^3 + (-15)^3 + (-13)^3 = 3xyz$$

$$= 0 + 3(28)(-15)(-13)$$

$$= 16380$$

**15. Give possible expressions for the length and breadth of each of the following rectangles, in which their areas are given:**

**(i) Area:  $25a^2 - 35a + 12$**

**(ii) Area:  $35y^2 + 13y - 12$**

Solution:

(i) Area:  $25a^2 - 35a + 12$

Using the splitting the middle term method,

We have to find a number whose sum =  $-35$  and product =  $25 \times 12 = 300$

We get -15 and -20 as the numbers  $[-15+-20=-35$  and  $-15\times-20 = 300]$

$$25a^2-35a+12 = 25a^2-15a-20a+12$$

$$= 5a(5a-3)-4(5a-3)$$

$$= (5a-4)(5a-3)$$

Possible expression for length =  $5a-4$

Possible expression for breadth =  $5a-3$

(ii) Area:  $35y^2+13y-12$

Using the splitting the middle term method,

We have to find a number whose sum = 13 and product =  $35\times-12 = 420$

We get -15 and 28 as the numbers  $[-15+28 = 13$  and  $-15\times28=420]$

$$35y^2+13y-12 = 35y^2-15y+28y-12$$

$$= 5y(7y-3)+4(7y-3)$$

$$= (5y+4)(7y-3)$$

Possible expression for length =  $(5y+4)$

Possible expression for breadth =  $(7y-3)$

**16. What are the possible expressions for the dimensions of the cuboids whose volumes are given below?**

**(i) Volume:  $3x^2-12x$**

**(ii) Volume:  $12ky^2+8ky-20k$**

Solution:

(i) Volume:  $3x^2-12x$

$3x^2-12x$  can be written as  $3x(x-4)$  by taking  $3x$  out of both the terms.

Possible expression for length =  $3$

Possible expression for breadth =  $x$

Possible expression for height =  $(x-4)$

(ii) Volume:

$12ky^2+8ky-20k$

$12ky^2+8ky-20k$  can be written as  $4k(3y^2+2y-5)$  by taking  $4k$  out of both the terms.

$$12ky^2+8ky-20k = 4k(3y^2+2y-5)$$

[Here,  $3y^2+2y-5$  can be written as  $3y^2+5y-3y-5$  using splitting the middle term method.]

$$= 4k(3y^2+5y-3y-5)$$

$$= 4k[y(3y+5)-1(3y+5)]$$

$$= 4k(3y+5)(y-1)$$

Possible expression for length =  $4k$

Possible expression for breadth =  $(3y + 5)$

Possible expression for height =  $(y - 1)$